

The 1<sup>st</sup> International Conference on Ubiquitous Security (UbiSec 2021)

The 6<sup>th</sup> International Workshop on Trusted Computing (IWTC 2021)

# Secure Search in Cloud Computing

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# Outline

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**Introduction**

**2**

**Previous Work**

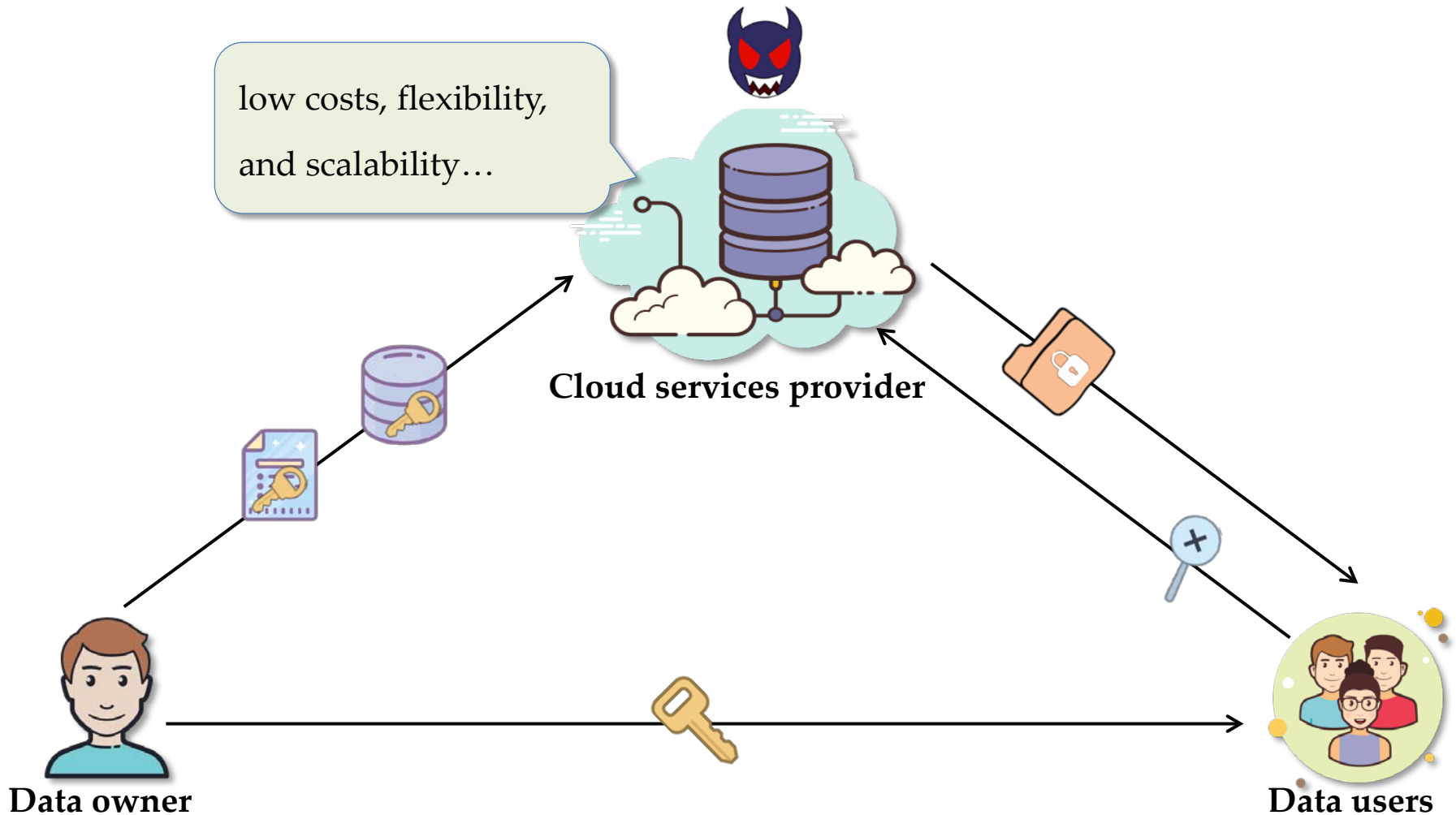
**3**

**Ongoing Work**

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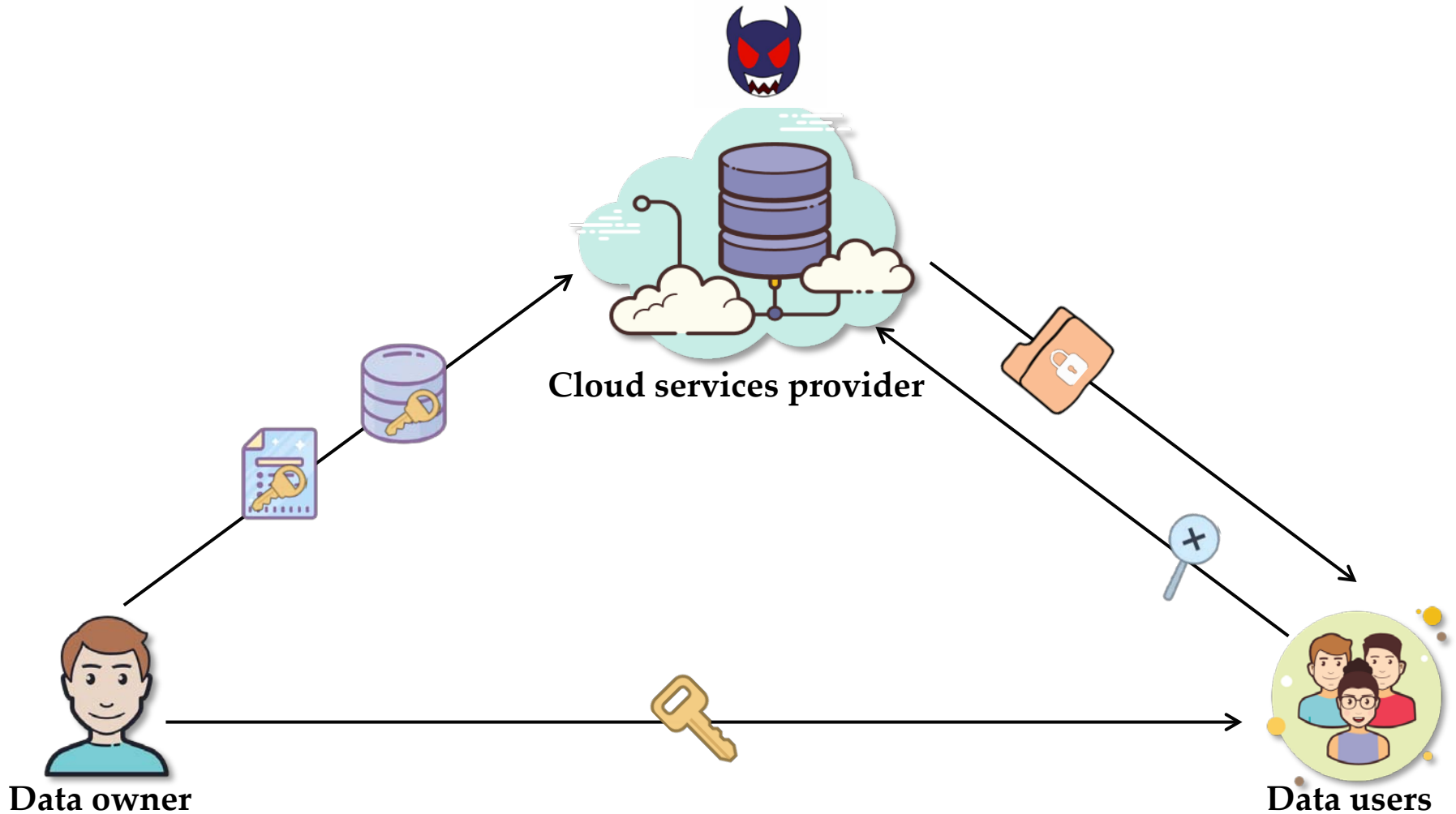
**Future Work**

# Introduction



- **Searchable encryption (SE)** is a tool that allows the cloud server to perform secure searches over encrypted data

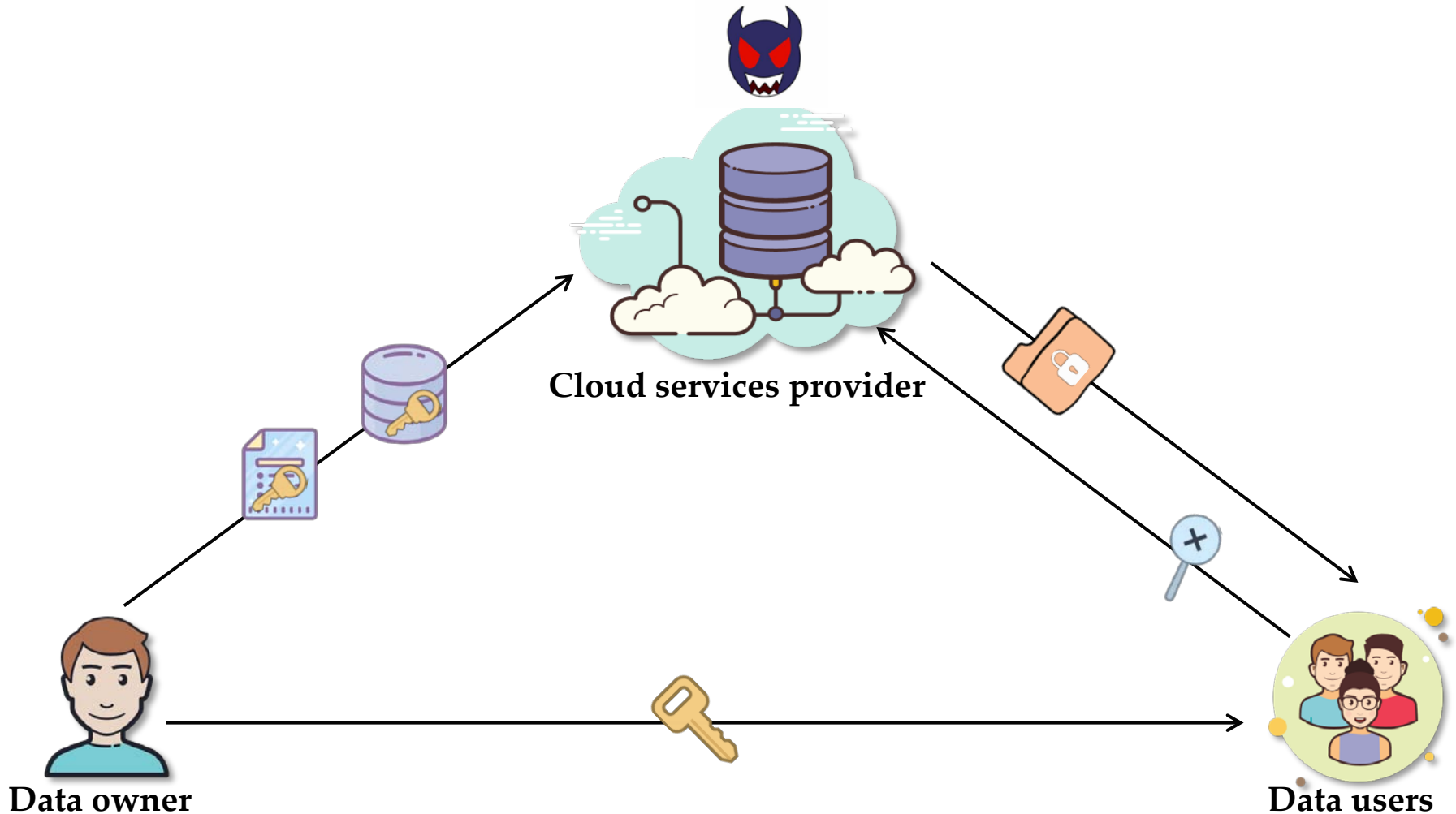
# Introduction



## Searchable Encryption

**Symmetric key setting:** the keys encrypting the index and the token are the same  
**Asymmetric key setting:** the keys encrypting the index and the token are different

# Introduction

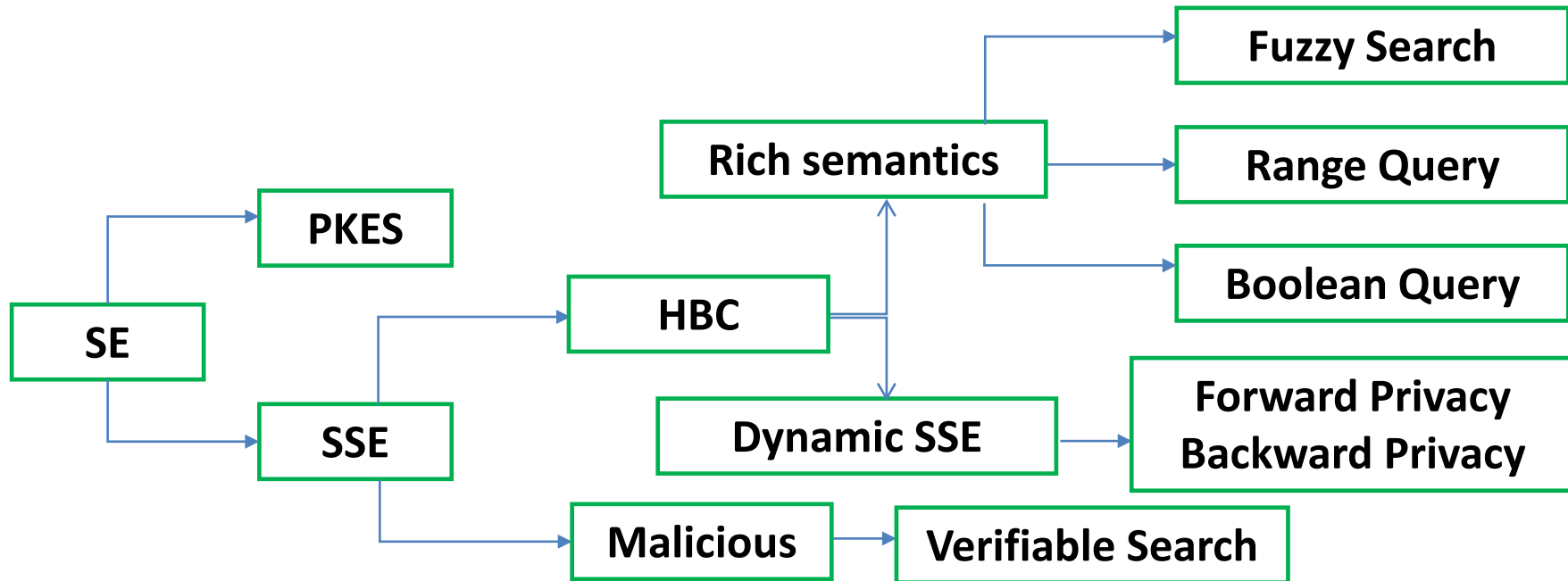


## Common Leakage in SSE

**Access pattern:** which files have been returned

**Search pattern:** whether two searches were performed for the same keyword

# Overview of Our Work



**Q. Liu**, Y. Peng, J. Wu, T. Wang, and G. Wang, "Secure Multi-Keyword Fuzzy Searches with Enhanced Service Quality in Cloud Computing" IEEE Transactions on Network and Service Management (TNSM), 2020.

**Q. Liu**, Y. Tian, J. Wu, T. Peng, and G. Wang, "Enabling Verifiable and Dynamic Ranked Search Over Outsourced Data," IEEE Transactions on Services Computing(TSC), 2019.

**Q. Liu**, X. Nie, X. Liu, T. Peng, and J. Wu, "Verifiable Ranked Search over Dynamic Encrypted Data in Cloud Computing," Proc. of IWQoS 2017.

based on Comparable Inner Product Encoding, Proc. of CNS 2018.

**L. Du**, K. Li\*, Q. Liu\*, Z. Wua, S. Zhang, "Dynamic Multi-Client Searchable Symmetric Encryption with Support for Boolean Queries, Information Sciences," 2019.

B. Hu, **Q. Liu**, X. Liu, T. Peng, G. Wang, J. Wu, "DABKS: Dynamic Attribute-based Keyword Search in Cloud Computing," Proc. of ICC 2017.



# Outline

**1**

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**Future Work**

# Prime Inner Product Encoding for Effective Wildcard-based Multi-Keyword Fuzzy Search

Qin Liu<sup>a</sup>, Yu Peng<sup>a</sup>, Shuyu Pei<sup>a</sup>, Jie Wu<sup>b</sup>, Tao Peng<sup>c</sup> and Guojun Wang<sup>c</sup>

<sup>a</sup> Hunan university

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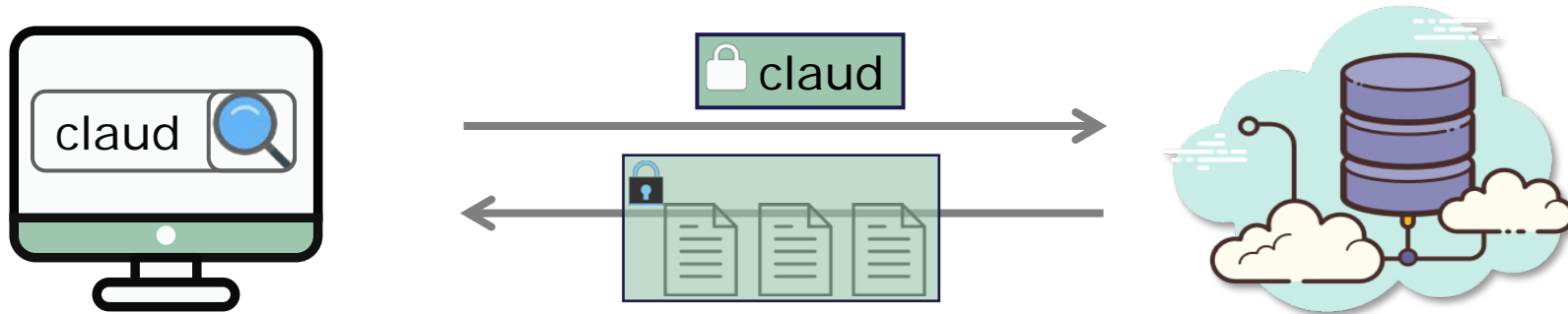
<sup>c</sup> Guangzhou university





# Introduction to Secure Fuzzy search

Alice wants to retrieve files containing keyword “cloud” from cloud servers.



The misspelling of a query keyword will cause an error result to be returned.

(claud v data)  $\wedge$  security

- **Fuzzy search.** The tolerance of misspelling of a keyword.
- **Flexibility.** The user can specify different search criteria.
- **Efficiency.** An efficient index structure to facilitate parallel searches.

## ● Inverted index

$O(r)$

$w_1$	ind1	ind2	ind3
$w_2$	ind2	ind3	
$w_3$	ind1	ind2	

# Related work on Secure Fuzzy Search

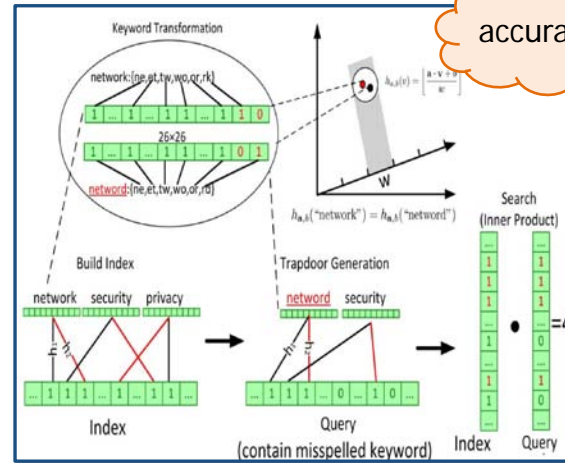
## INFOCOM2010 [1]

$S_{CASTLE}$   
 = {CASTLE, \* CASTLE,  
 \* ASTLE, C \* ASTLE, C  
 \* STLE, ..., CASTL \* E, CASTL  
 \*, CASTLE \*}

single keyword,  
predefined set

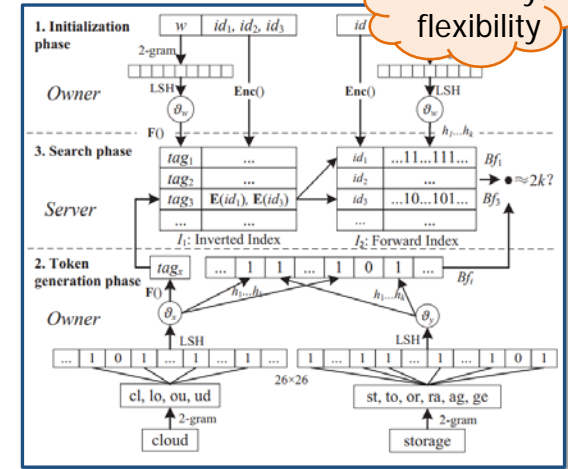
Pre-set edit distance = 1

## INFOCOM2014 [2]



accuracy

## TSC2017 [4]



accuracy,  
flexibility

Schemes	Multi-keyword fuzzy Search	Flexibility	Indexes	Building blocks
INFOCOM2010 [1]	✗	-	-	Predefined set
INFOCOM2014 [2]	✓	✗	Forward index	LSH, bloom filter
TIFS2016 [3]	✓	✗	Forward index	LSH, bloom filter
TSC2017 [4]	✓	✗	Forward + inverted index	LSH, bloom filter
TDSC2019 [5]	✓	✗	tree	-
JNCA2020 [6]	✓	✗	tree	LSH, bloom filter

# Contributions of Our Work

## The Prime Inner Product Encoding (PIPE) Scheme

### Main idea

- Encoding a query keyword or an index keyword into a vector filled with primes or reciprocals of primes, such that the result of vectors' inner product is an integer only when two keywords are similar.

### Compared with Previous Fuzzy Search Schemes

- **Greater flexibility.** Vectors are organized into prime-related matrices to support multi-semantic queries.
- **Higher efficiency.** A keyword balanced binary (KBB) tree is built to support parallelizable and dynamic search.
- **Enhanced robustness.** A query matrix is extended by random noises to resist linear analysis attacks.


# Basic scheme: Prime Inner Product Encoding (PIPE<sub>0</sub>)

Files	keywords
$D_1$	{"hello", "key"}

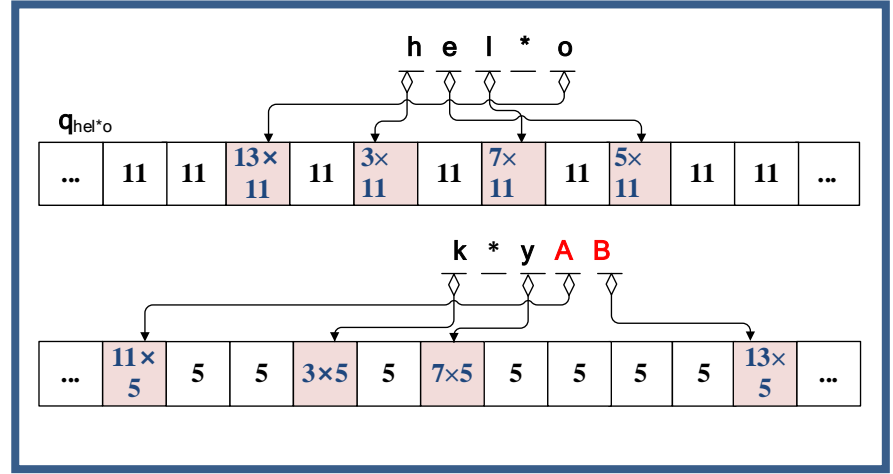
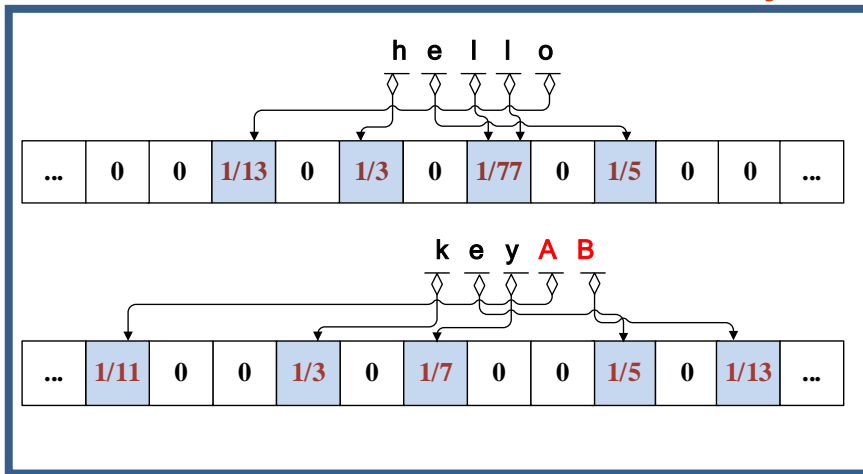
$\mathcal{P}$  (3, 5, 7, 11, 13)

Max length of universal keywords  $L = 5$

(A, B, C, D, E)

hel\*o, k\*y 

Dummy characters



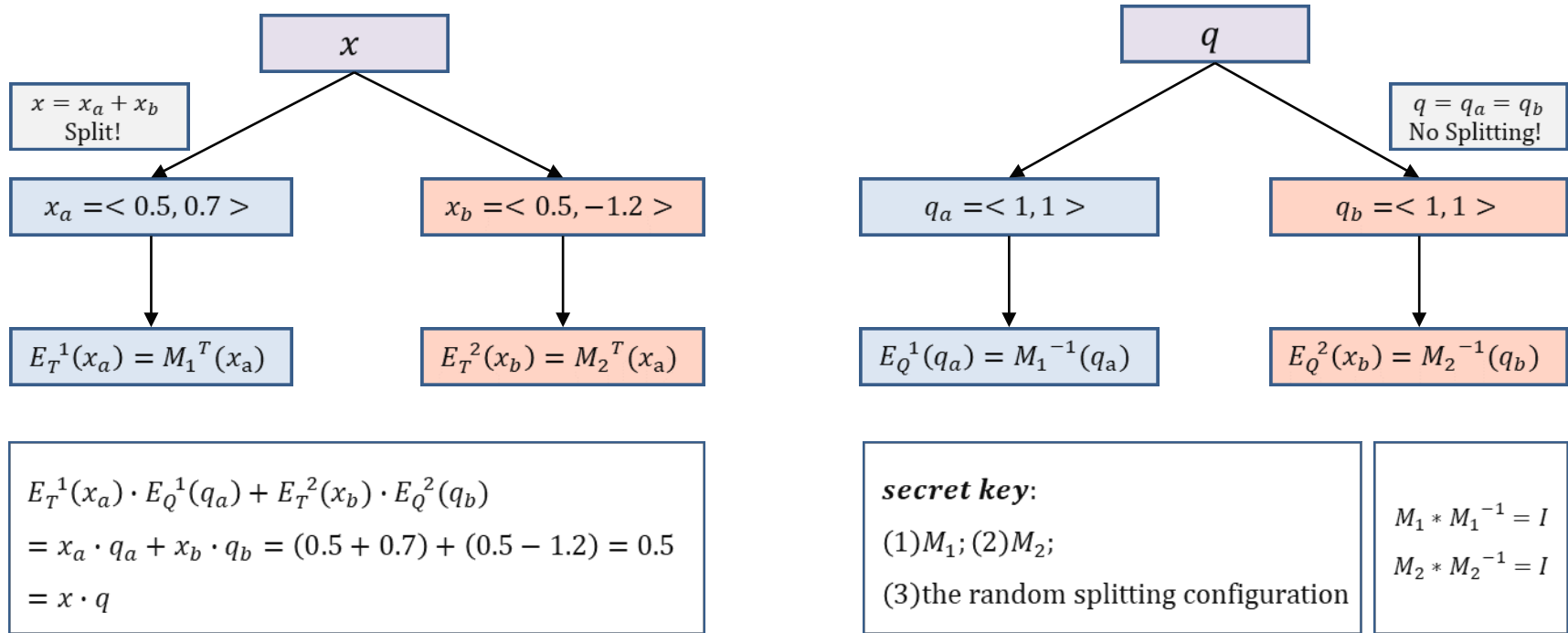
- The inner products between the index vectors and the query vectors

$$R = \begin{cases} \mathbf{p}_{hello} \cdot \mathbf{q}_{hel*o} = 34, & \mathbf{p}_{hello} \cdot \mathbf{q}_{k*y} \approx 3.11 \\ \mathbf{p}_{hello} \cdot \mathbf{q}_{k*y} = 3.12, & \mathbf{p}_{key} \cdot \mathbf{q}_{k*y} \approx 21 \end{cases}$$

- For AND queries, if each column of  $R$  has at least one integer, the query  $q$  matches the file  $D$
- For OR queries, if at least one element in  $R$  is an integer, the query  $q$  matches the file  $D$

# Secure KNN

$x = \langle 1, -0.5 \rangle, q = \langle 1, 1 \rangle$ ; ensure  $x \cdot q = 0.5$  can be recovered on E(DB)



- The multiplication of the plaintext matrices to be calculated based on their encrypted forms.

# Advanced scheme: PIPE<sub>S</sub>

- Secure KNN failed to resist linear analyses. [ICDE2013 \[6\]](#)

$$\mathbf{A}_1 = \begin{bmatrix} \mathbf{p}_{hello} \\ \mathbf{p}_{key} \end{bmatrix}$$

$$\mathbf{B}_1 = [\mathbf{q}_{hel*o} \quad \mathbf{q}_{k*y}] \xrightarrow{\quad} \mathbf{B}_1 =$$

$\mathbf{Q}_{hel*o}$			$\mathbf{Q}_{k*y}$		
$\mathbf{q}_{hel*o}[1]$	$X_{1,2}$	$X_{1,3}$	$\mathbf{q}_{k*y}[1]$	$X_{1,5}$	$X_{1,6}$
$X_{2,1}$	$\mathbf{q}_{hel*o}[2]$	$X_{2,3}$	$X_{2,4}$	$\mathbf{q}_{k*y}[2]$	$X_{2,6}$
$X_{3,1}$	$X_{3,2}$	$\mathbf{q}_{hel*o}[3]$	$X_{3,4}$	$X_{3,5}$	$\mathbf{q}_{k*y}[3]$
$\mathbf{q}_{hel*o}[4]$	$X_{4,2}$	$X_{4,3}$	$X_{4,4}$	$X_{4,5}$	$\mathbf{q}_{k*y}[4]$
...	...	...	...	...	...
$\mathbf{q}_{hel*o}[d]$	$X_{d,2}$	$X_{d,3}$	$X_{d,4}$	$X_{d,5}$	$\mathbf{q}_{k*y}[d]$

$$\mathbf{R}_{1,1} = \begin{bmatrix} \sum_{i=1}^s \mathbf{r}_{1,1}[i] & \sum_{i=1}^s \mathbf{r}_{1,2}[i] \\ \sum_{i=1}^s \mathbf{r}_{2,1}[i] & \sum_{i=1}^s \mathbf{r}_{2,2}[i] \end{bmatrix}$$

$$\mathbf{R}_{1,1} = \mathbf{A}_1 \star \mathbf{B}_1 =$$

$\mathbf{r}_{1,1}$			$\mathbf{r}_{1,2}$		
$\mathbf{p}_{hello} \cdot \mathbf{Q}_{hel*o}[*][1]$	$\mathbf{p}_{hello} \cdot \mathbf{Q}_{hel*o}[*][2]$	$\mathbf{p}_{hello} \cdot \mathbf{Q}_{hel*o}[*][3]$	$\mathbf{p}_{hello} \cdot \mathbf{Q}_{k*y}[*][1]$	$\mathbf{p}_{hello} \cdot \mathbf{Q}_{k*y}[*][2]$	$\mathbf{p}_{hello} \cdot \mathbf{Q}_{k*y}[*][3]$
$\mathbf{p}_{key} \cdot \mathbf{Q}_{hel*o}[*][1]$	$\mathbf{p}_{key} \cdot \mathbf{Q}_{hel*o}[*][2]$	$\mathbf{p}_{key} \cdot \mathbf{Q}_{hel*o}[*][3]$	$\mathbf{p}_{key} \cdot \mathbf{Q}_{k*y}[*][1]$	$\mathbf{p}_{key} \cdot \mathbf{Q}_{k*y}[*][2]$	$\mathbf{p}_{key} \cdot \mathbf{Q}_{k*y}[*][3]$
$\mathbf{r}_{2,1}$			$\mathbf{r}_{2,2}$		

- Each column of matrix  $Q$  contains at least one element of vector  $q$ .
- The sum of the random numbers at the  $l$ -th row, denoted as  $\delta_l$ , is equal to  $t_l q[l]$  where  $t_l = 0$  or  $(t_l + 1)$  is a prime outside primes set  $\mathcal{P}$ .

$\alpha = p \cdot q + X$ , where  $X \in R$  is a random number that has no linear relationship with the result of  $p \cdot q$ . Therefore, it is impossible for the adversary to decompose  $p \cdot q$  from  $\alpha$ .

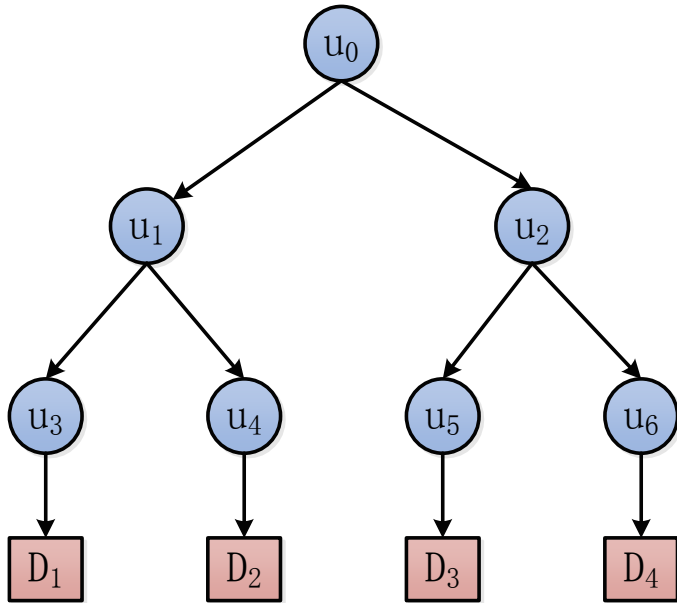
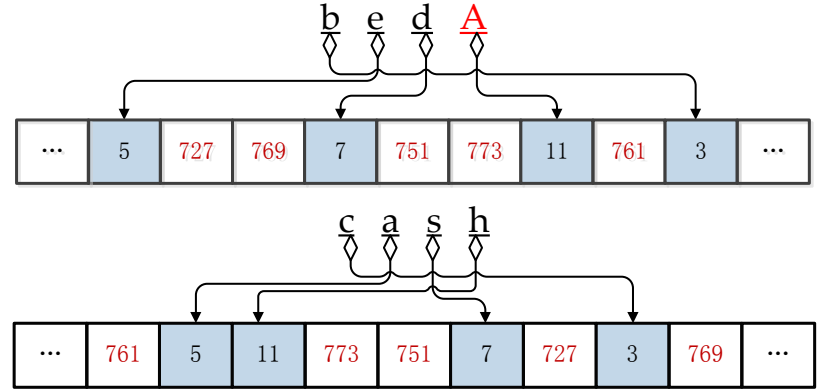
# Tree-based Index

Files	keywords
$D_1$	{"bed", "cash"}
$D_2$	{"cash"}
$D_3$	{"cat", {"pen"}}
$D_4$	{"love"}

Max length of universal keywords  $L = 4$

$\mathcal{P}$  (3, 5, 7, 11)

(A, B, C, D)



$u_3$ . data

...	5	727	769	7	751	773	11	761	3	...
...	761	5	11	773	751	7	727	3	769	...

$u_4$ . data

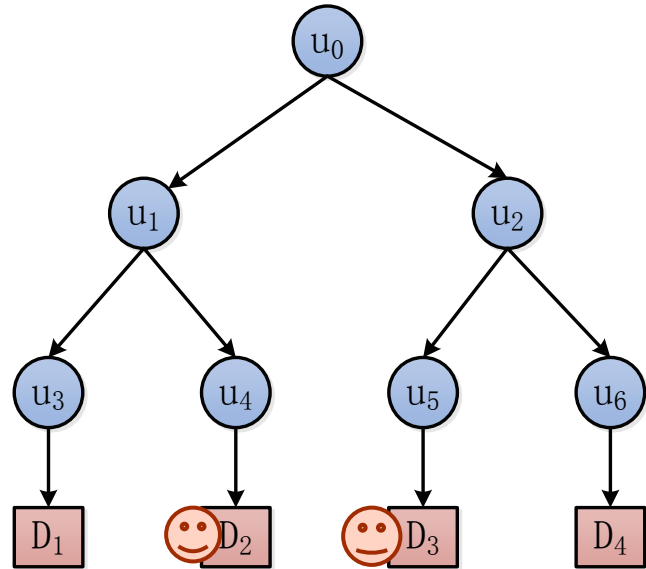
...	761	5	11	773	751	7	727	3	769	...
...	1	1	1	1	1	1	1	1	1	...

$u_1$ . data

...	$5 \times$	$727$	$769$	$7 \times$	751	773	$11 \times$	$761$	$3 \times$	...
...	761	$\times 5$	$\times 11$	773	$\times 7$	$\times 727$	$\times 3$	769	...	
...	761	5	11	773	751	7	727	3	769	...

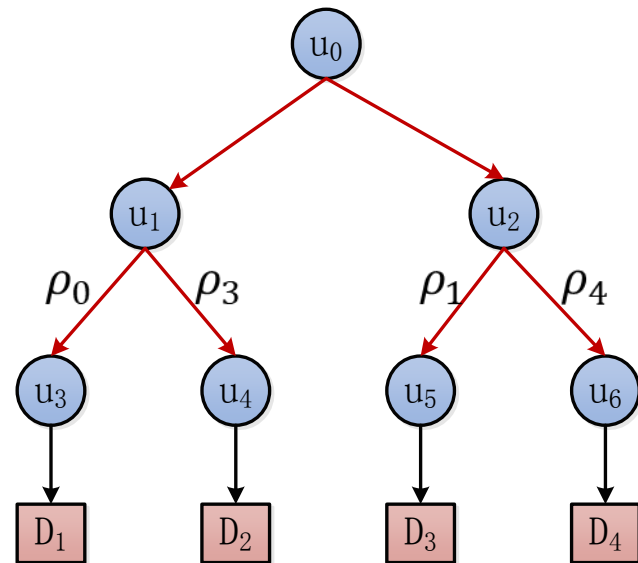
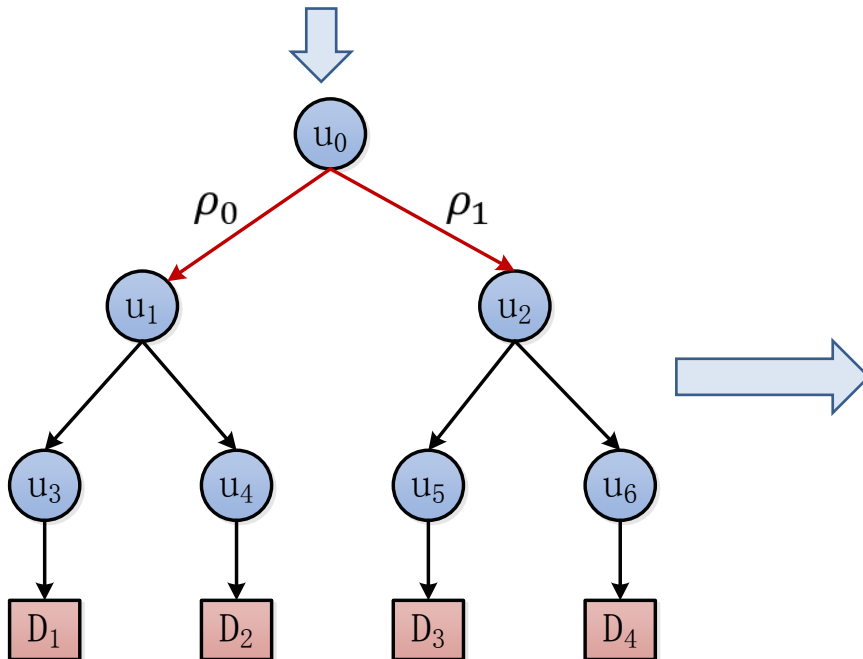
$U = \langle \text{nid}, \text{data}, \text{fid}, \text{lchild}, \text{rchild} \rangle$

# Parallel search



Let  $P = \{\rho_0, \rho_1, \rho_2, \rho_3\}$  be a set of 4 available processors in the system

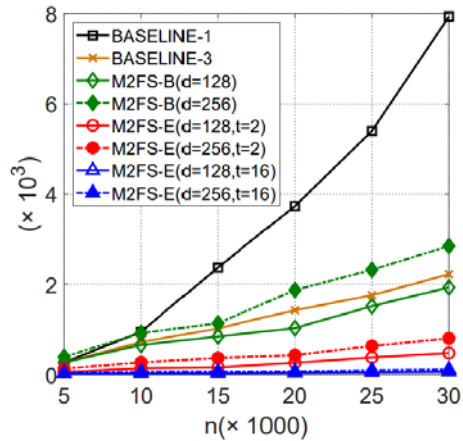
$$O\left(\frac{r \log n}{t}\right)$$



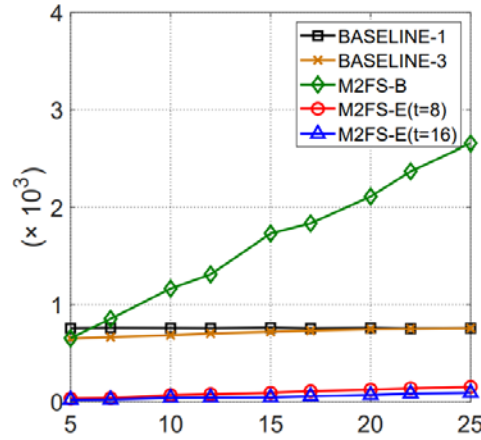


# Evaluation

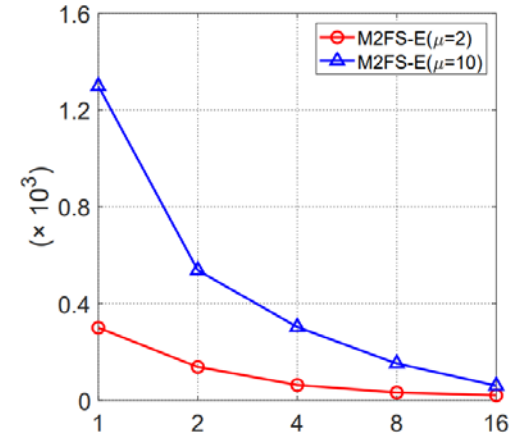
## ● Comparison of the execution time (*ms*) for AND queries



(a) The time for searching  $n$  files

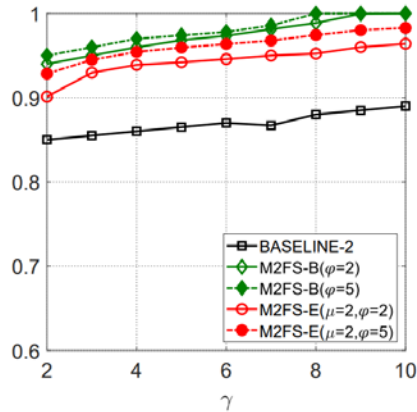


(b) The time for searching  $\gamma$  keywords

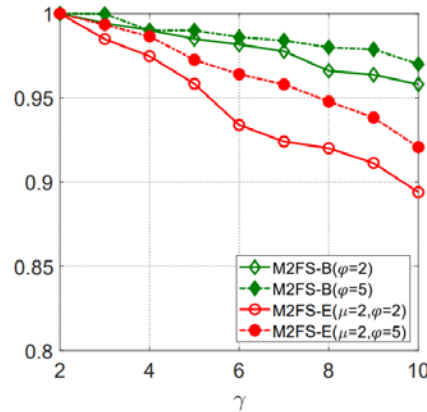


(c) The search time  $t$  under different  $\mu$

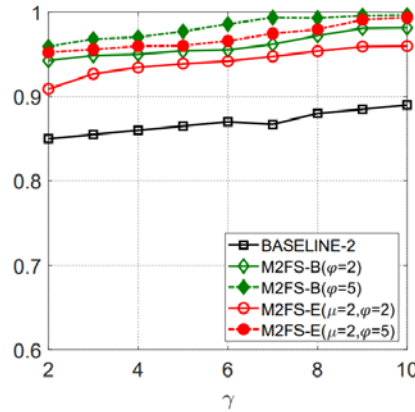
## ● Comparison of the execution time (*ms*) for AND queries



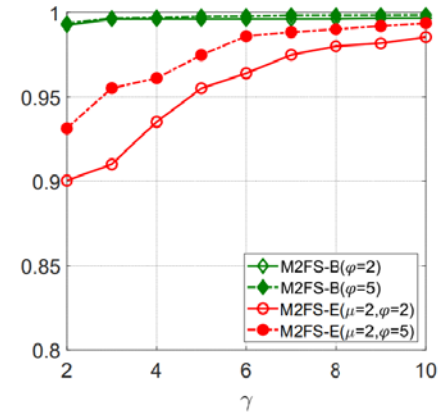
(a) Precision of AND queries



(b) Recall of AND queries



(c) Precision of OR queries



(d) Recall of OR queries

# References

- [1] J. Li, Q. Wang, C. Wang, N. Cao, K. Ren, and W. Lou, “Fuzzy keyword search over encrypted data in cloud computing,” in Proc. of INFOCOM, 2010. . [\[INFOCOM2010\]](#)
- [2] B. Wang, S. Yu, W. Lou, and Y. T. Hou, “Privacy-preserving multikeyword fuzzy search over encrypted data in the cloud,” in Proc. of INFOCOM, 2014. [\[INFOCOM2014\]](#)
- [3] Z. Fu, X. Wu, C. Guan, X. Sun, and K. Ren, “Toward efficient multi-keyword fuzzy search over encrypted outsourced data with accuracy improvement,” IEEE Transactions on Information Forensics and Security, 2016. [\[TIFS2016\]](#)
- [4] J. Chen, K. He, L. Deng, Q. Yuan, R. Du, Y. Xiang, and J. Wu, “EliMFS: achieving efficient, leakage-resilient, and multi-keyword fuzzy search on encrypted cloud data,” IEEE Transactions on Services Computing, 2017. [\[TSC2017\]](#)
- [5] Q. Liu, Y. Peng, S. Pei, J. Wu, T. Peng and G. Wang, "Prime Inner Product Encoding for Effective Wildcard-based Multi-Keyword Fuzzy Search," IEEE Transactions on Services Computing, 2020. [\[TSC2020\]](#)
- [6] B. Yao, F. Li, and X. Xiao, “Secure nearest neighbor revisited,” in Proc. of ICDE, 2013. [\[ICDE2013\]](#)

# Secure and Efficient Multi-Attribute Range Queries based on Comparable Inner Product Encoding

Qin Liu<sup>a</sup>, SiXia Wu<sup>a</sup>, Shuyu Pei<sup>a</sup>, Jie Wu<sup>b</sup>, Tao Peng<sup>c</sup> and Guojun Wang<sup>c</sup>

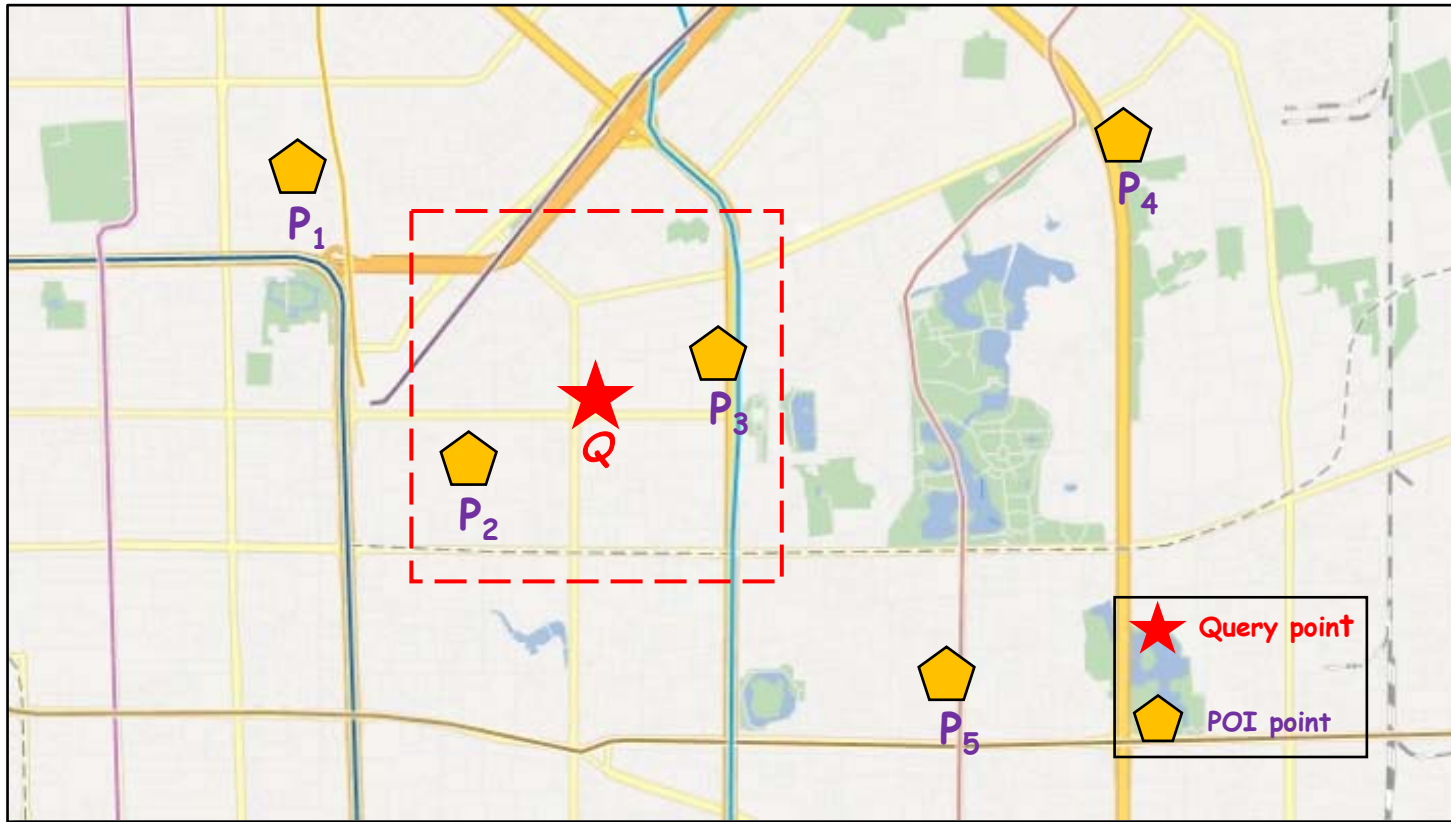
<sup>a</sup> Hunan university

<sup>b</sup> Temple university

<sup>c</sup> Guangzhou university



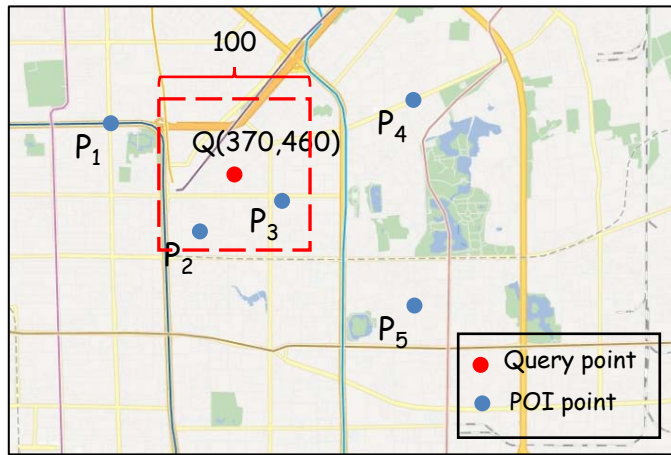
# Introduction to Secure Range Query



## Location based services(LBS)

- LBS uses of location technology to obtain the current location of the device and provides query services through the mobile Internet.
- E.g. **range query** or ***k*NN query**.

# Introduction to Secure Range Query



Point	x-coordinate	y-coordinate
$P_1$	300	480
$P_2$	350	420
$P_3$	400	440
$P_4$	450	520
$P_5$	450	300

- 2-dimensional range query is used in Location Based Services(LBS).
- E.g.  $Q=(370, 460)$  and edge length = 100, the result of range query is  $\{P_2, P_3\}$ .
- Besides, multi-dimensional range query has wide application prospect.
  - (Age in [20,40] AND Blood Pressure in [100, 130] AND Weight in [60, 80] )

Challenge in secure range query: Comparisons need to be performed based on ciphertextes!

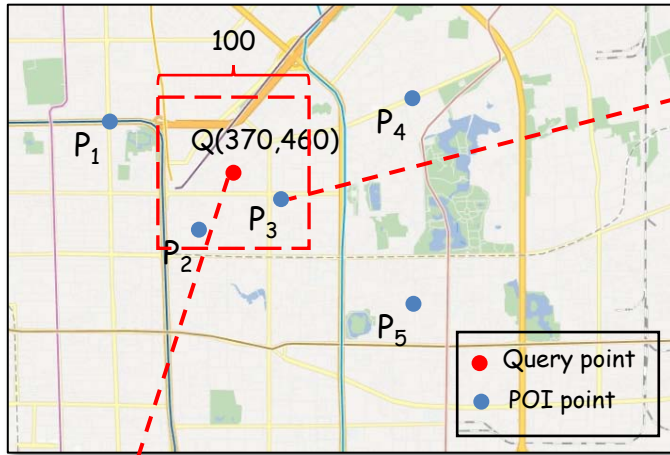
# Related work on Secure Range Query

Schemes	Efficiency	Scalability	Security	Privacy
Most of OPE	✓	✓	x	✓
Ideal OPE	x	✓	✓	✓
ORE	✓	✓	x	✓
Homomorphic	x	✓	✓	✓
CIPE scheme	✓	✓	✓	✓

## Contributions

- **Enhanced security.** It can resist inference attacks that existing OPE schemes are vulnerable to.
- **Higher efficiency.** It needs only around **1.4s** on average while performing two-attribute range queries on **1 million** encrypted data records.

# Basic Scheme: CIPE<sub>0</sub>



$P_3(400,440)$

$\mathbf{p}_{3x}$	400	400	1	1
-------------------	-----	-----	---	---

$\mathbf{p}_{3y}$	440	440	1	1
-------------------	-----	-----	---	---

Index vector constructions

$$\mathbf{p}_{3x} \cdot \mathbf{q}_{xl} = 2 \times (-400 + 320) < 0$$

$$\mathbf{p}_{3x} \cdot \mathbf{q}_{xu} = 2 \times (-400 + 420) > 0$$

$$\mathbf{p}_{3y} \cdot \mathbf{q}_{yl} = 2 \times (-440 + 310) < 0$$

$$\mathbf{p}_{3y} \cdot \mathbf{q}_{yu} = 2 \times (-440 + 510) \geq 0$$



Query([320,420], [410,510])

$\mathbf{q}_{xl}$	-1	-1	320	320
-------------------	----	----	-----	-----

$\mathbf{q}_{xu}$	-1	-1	420	420
-------------------	----	----	-----	-----

$\mathbf{q}_{yl}$	-1	-1	410	410
-------------------	----	----	-----	-----

$\mathbf{q}_{yu}$	-1	-1	510	510
-------------------	----	----	-----	-----

Query vector constructions



- The distance between attribute values
- The equality of attribute values

Noise addition!

$$v_{k,l} = p_{i_k} \cdot q_{j_{k,l}} = (\sum C + \sum \bar{C})(b_{j_{k,l}} - a_{i_k}) > 0$$

# Advanced scheme: CIPE<sub>S</sub>

- Secure KNN has been proved unable to resist chosen plaintext attacks(CPA)

$$p \cdot q = p'_{|\alpha|} \cdot q'_{|\alpha|} + p'_{|\beta|} \cdot q'_{|\beta|}$$

Extend  
Query matrices!

$$\bar{C} = (0.5, 0) \quad \begin{bmatrix} -0.5 & 0 & 165 & 0 & 330 & 330 & -1 & -1 \end{bmatrix} \quad \mathbf{q}_{1,l}$$

$$\bar{C} = (0, 0.01) \quad \begin{bmatrix} 0 & -0.01 & 0 & 4.3 & 430 & 430 & -1 & -1 \end{bmatrix} \quad \mathbf{q}_{1,u}$$

-0.15	1.105	-1	0	1	0	-1	2	4	-3	-3
-2	0	2	-2	-0.02	0.006	-1	1	-4	5	1
-2	-32.65	49.5	3.1	1	0	-2.58	1.9	-2	-3	-1
0	-3	3	-5	-3	-2	8.6	0	10	0	0
99	-63.3	-6	2	4	-3	-258	860	-3	-1	1
99	-300	230.7	2.5	3.5	-4	-1	-258	860	1.5	-2.5
-0.3	0.21	0	3	-6	3	-0.5	-1.5	0.6	-2	2
-0.3	0	0.21	3	-3	0	1	-4	3	0.6	-2

(a)  $\mathbf{Q}_{1,l}$  ( $d=8, s=3$ ).

Set  $r = 0.3$  and  $t = -0.21$

(b)  $\mathbf{Q}_{1,u}$  ( $d=8, s=8$ ).

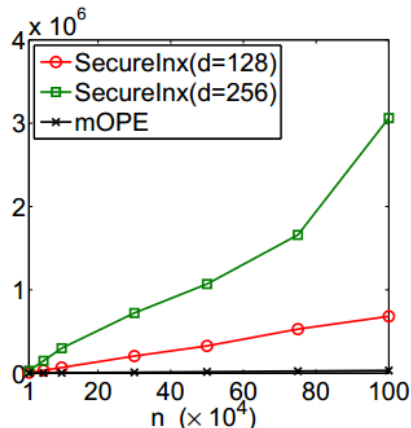
Set  $r = 2$  and  $t = -0.6$

$$p \cdot q \neq p'_{|\alpha|} \cdot q'_{|\alpha|} + p'_{|\beta|} \cdot q'_{|\beta|}$$

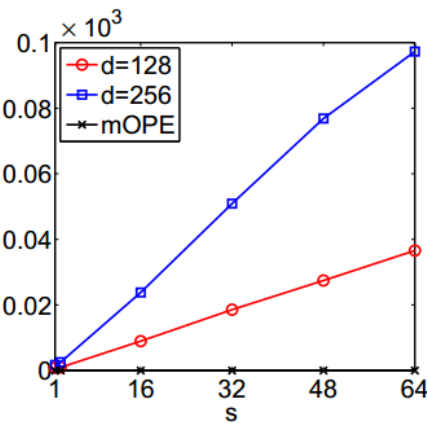


# Evaluation

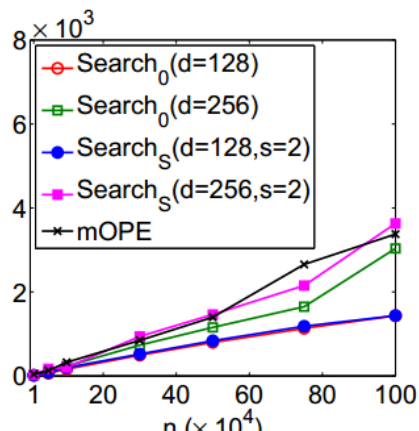
- Comparison of the execution time (ms) between CIPE and mOPE



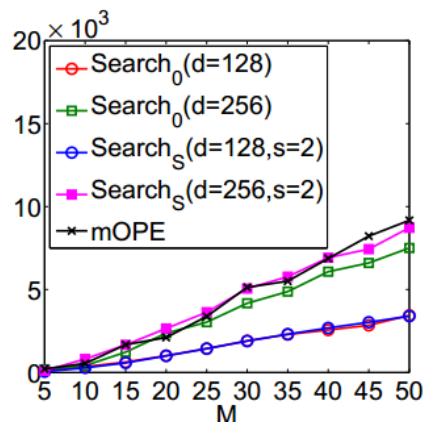
(a) Index generation time.



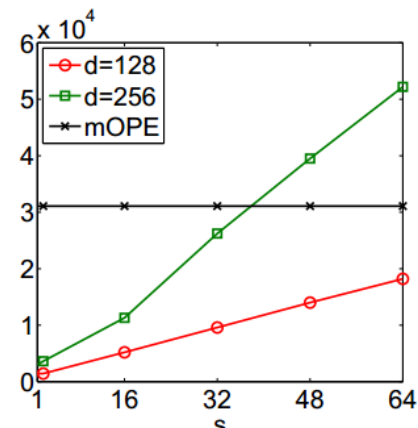
(b) Trapdoor generation time.



(c) Search time.



(d) Search time.



(e) Search time.



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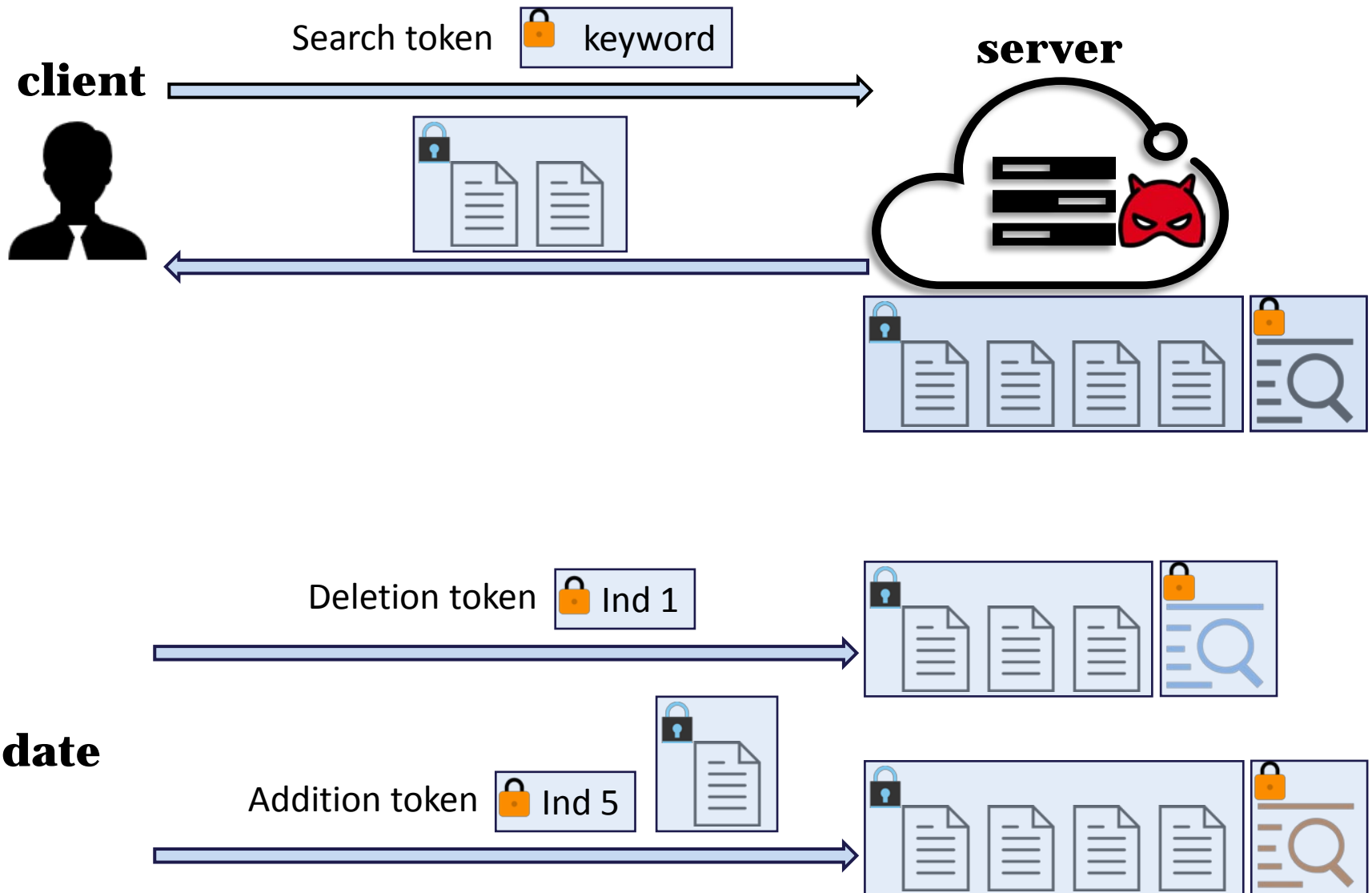
**Future Work**



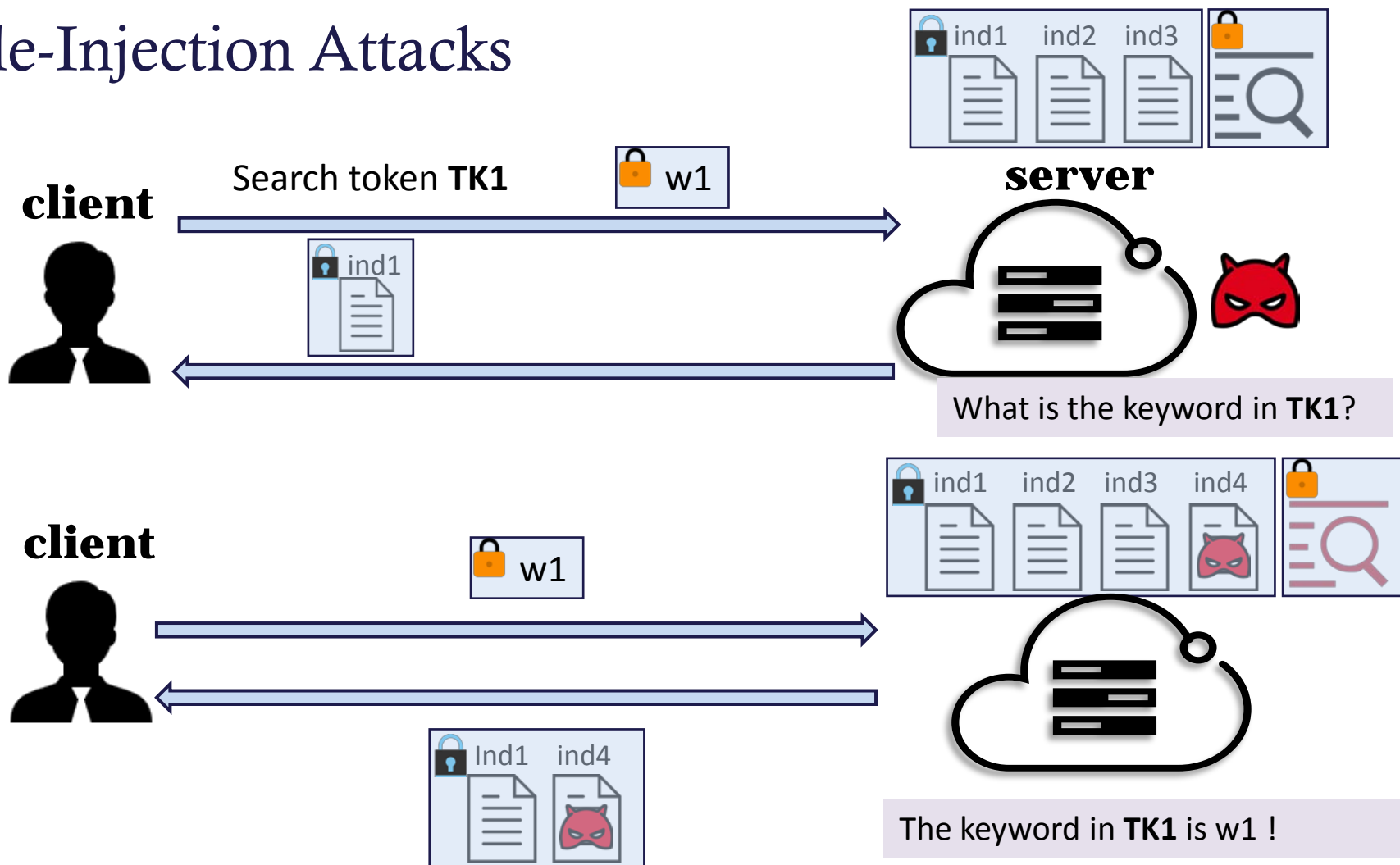
## Forward and Backward Privacy of DSSE

Qin Liu<sup>a</sup>, Yu Peng<sup>a</sup>, Hongbo Jiang<sup>a</sup>, Guojun Wang<sup>b</sup>, Tian Wang<sup>c</sup>, and Jie Wu<sup>d</sup>

# Dynamic searchable symmetric encryption (DSSE)



# File-Injection Attacks



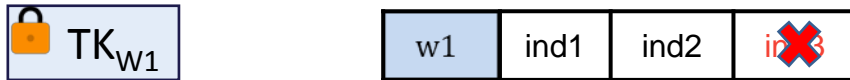
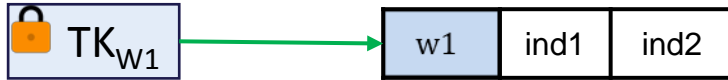
## ○ Why query privacy is important?

- Keywords are part of the files. File content can be recovered.
- Keywords can be used to classify files and help **other attacks**.

**Forward Privacy is required in DSSE to resist file injection attack !**

# Forward Privacy (FP)

- **Forward privacy (FP)** requires that the newly added files cannot be linked to previous search tokens.



Chang et al.[1]

- The first FP construction
- High communication cost due to the ever-growing query size

2005

Stefanov et al.[2]

- The first FP scheme with sublinear search time
- Based on oblivious RAM
- High communication cost

2014

Bost et al.[3]

- Formally defined forward privacy
- Low communication cost
- High computation cost of asymmetric cryptography

2016

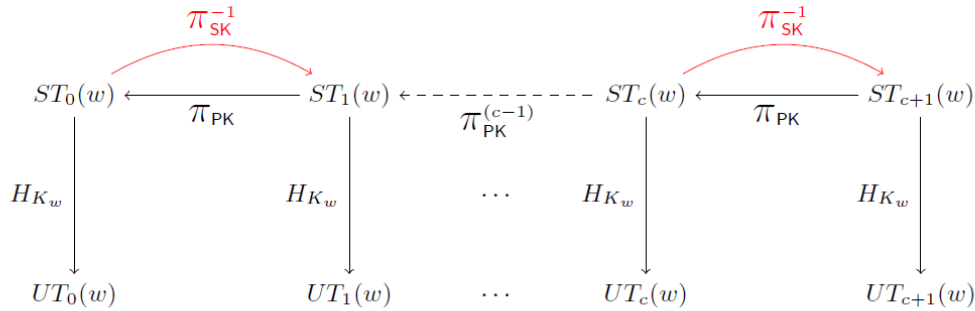
[1] Chang et al. "Privacy preserving keyword searches on remote encrypted data." in Proc. ACNS, 2005.

[2] Stefanov et al. "Practical Dynamic Searchable Encryption with Small Leakage." in Proc. NDSS, 2014.

[3] Bost et al. "Σοφος: Forward secure searchable encryption." in Proc. CCS, 2016.

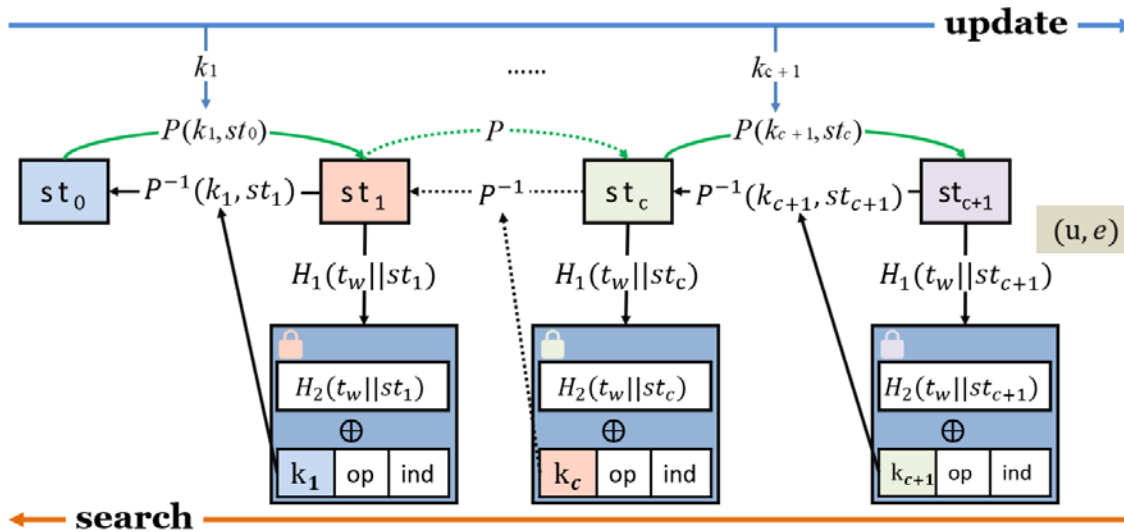
# State-of-the-art FP Schemes

- Sophos: Trapdoor permutation (TDP)



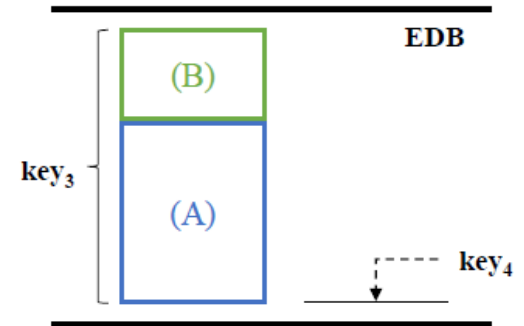
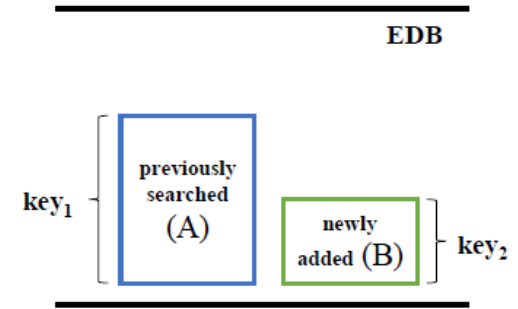
Relations among tokens. Operations in red can only be done by the client, using the secret key SK

- Fast: Pseudorandom permutation (symmetric primitives)



Lack of actual deletion

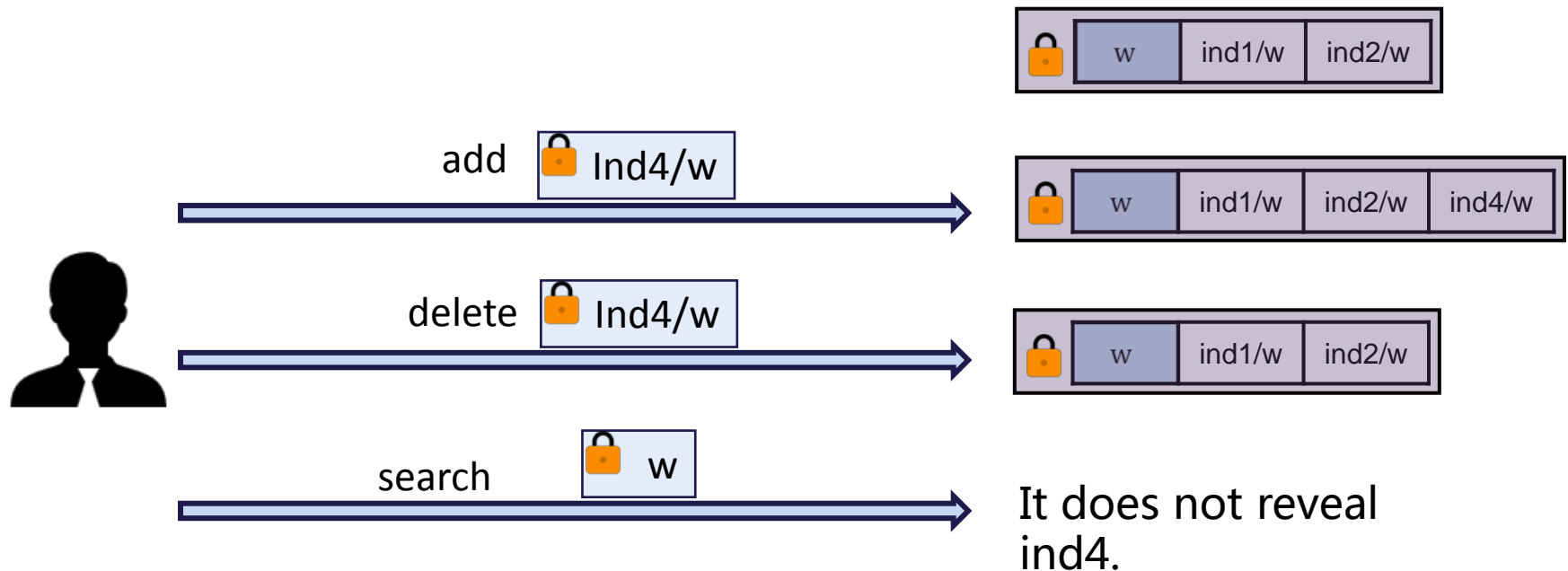
- Dual dictionary



Re-Encryption  
Storage cost

# Backward Privacy (BP)

- **Backward privacy (BP):** the deleted files cannot be searched any more.



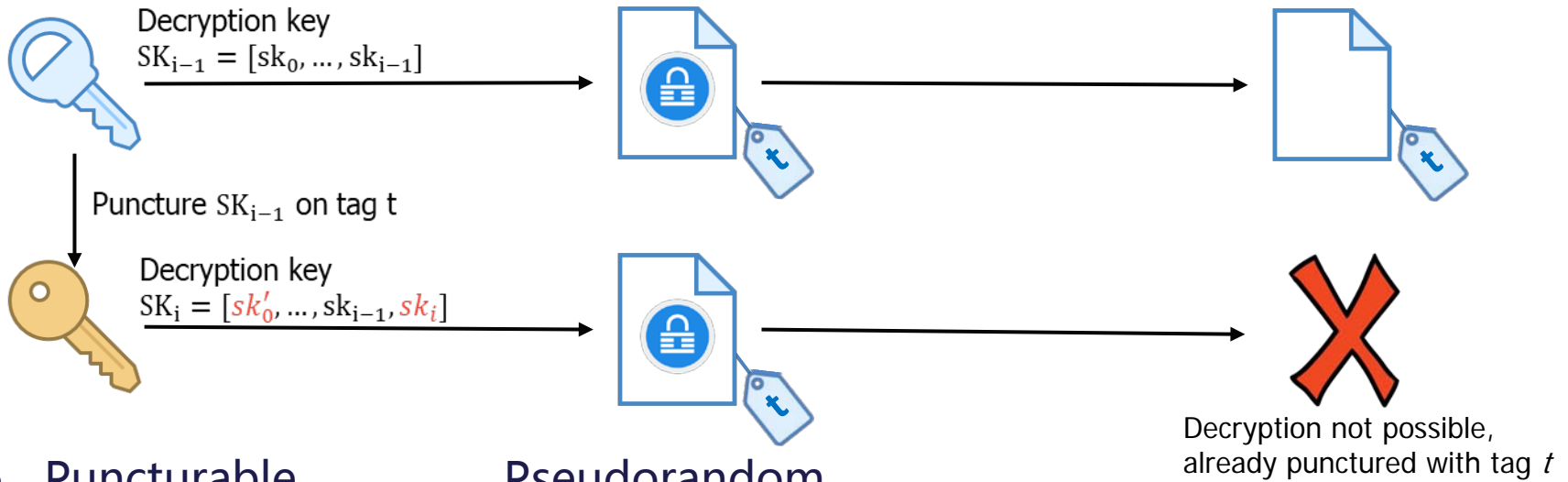
- Backward privacy: the deleted files cannot be searched.

[1] Bost, Raphaël, Brice Minaud, and Olga Ohrimenko. "Forward and backward private searchable encryption from constrained cryptographic primitives," in Proc. of CCS, 2017.

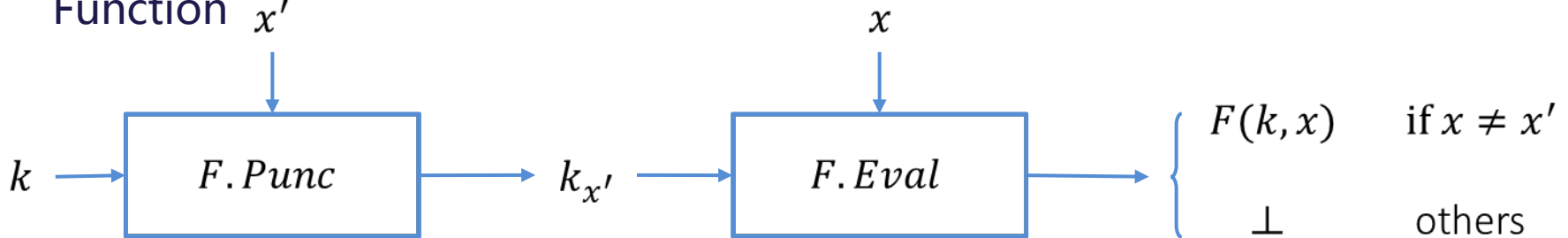


# State-of-the-art- BP Schemes

- Constrained pseudorandom function (CPRF)
- Public-key Puncturable Encryption



- Puncturable Function  $x'$
- Pseudorandom



- Symmetric Puncturable Encryption (SPE)
- FP + 2 round trip

# Related Work on Forward & Backward Privacy

Schemes	Forward privacy	Backward privacy	Search round trip	Building blocks
Sophos [1]	√	✗	-	Trapdoor permutation
FAST [2]	√	✗	-	Pseudorandom function
Dual [3]	√	✗	-	Dual dictionary
Diana <sub>del</sub> [4]	√	BP-3	2	Constrained pseudorandom functions
Janus [4]	√	BP-3	1	Puncturable encryption
Janus++ [6]	√	BP-3	1	Symmetric puncturable encryption
Fish-bone [7]	√	BP-3	2	Symmetric key encryption
Fides [4]	√	BP-2	2	From Sophos
Mitra [8]	√	BP-2	2	-
Moneta [4]	√	BP-1	3	obvious RAM
Orion [8]	√	BP-1	$O(\log N)$	obvious RAM

# Our Scheme with FP & BP

- **Basic scheme (FP)**

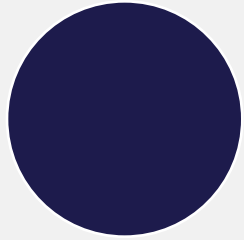
- **A hybrid index structure** that incorporates the merits of both inverted indexes and forward indexes, but is much more simple and efficient.

- **Advanced scheme (FP+BP)**

- Hybrid index + Symmetric Puncturable Encryption (SPE)
- File-based BP

<i>ind</i>	<i>head<sup>ind</sup></i>
ind1	
ind2	
...	





Thanks for your attentions

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